## edexcel 쁯

Mark Scheme (Results)
January 2017
Pearson Edexcel
International A-Level Mathematics
Decision Mathematics 1 (WDM01)

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## General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.


## EDEXCEL GCE MATHEMATICS

## General Instructions for Marking

1. The total number of marks for the paper is 75 .
2. The Edexcel Mathematics mark schemes use the following types of marks:

- M marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- B marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.

3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod - benefit of doubt
- ft - follow through
- the symbol $\sqrt{ }$ will be used for correct ft
- cao - correct answer only
- cso - correct solution only. There must be no errors in this part of the question to obtain this mark
- isw - ignore subsequent working
- awrt - answers which round to
- SC: special case
- oe - or equivalent (and appropriate)
- dep - dependent
- indep - independent
- dp decimal places
- sf significant figures
-     * The answer is printed on the paper
- The second mark is dependent on gaining the first mark

4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.
5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any $A$ or $B$ marks gained, in that part of the question affected.
6. If a candidate makes more than one attempt at any question:

- If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
- If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.

7. Ignore wrong working or incorrect statements following a correct answer.

| Question <br> Number | Scheme | Marks |
| :---: | :--- | :--- |
| $\left[\frac{1+10}{2}\right]=6$ Noether - reject $6-10$ | M1 |  |
| 1. | $\left[\frac{1+5}{2}\right]=3$ Gauss - reject $1-3$ <br> $\left[\frac{4+5}{2}\right]=5$ Lagrange - reject 5 | A1 |
| $[4]=4$ Hamilton (reject 4) |  |  |
| Hilbert not in list | A1cso (4) |  |

## Notes for Question 1

1M1: Choosing middle right pivots (choosing middle left is M0) + an attempt at discarding/retaining half the list

1A1: First pass correct i.e. $6^{\text {th }}$ item and using $1-5$ in the second pass (must not be using the $6^{\text {th }}$ item in the second pass)

2A1: Second and third passes correct i.e. $3^{\text {rd }}(\mathrm{G})$ and $5^{\text {th }}(\mathrm{L})$ items (no sticky pivots) - need not be rejecting the $5^{\text {th }}$ item for this mark

3A1: CSO search complete (so rejecting $5^{\text {th }}$ and $4^{\text {th }}$ items (which in the case of the $4^{\text {th }}$ item may be implicit)) + 'not found' - must be a clear distinction between Hamilton and Hilbert

| Question <br> Number | Scheme | Marks |  |
| :---: | :---: | :---: | :---: |
| 2. (a) | $\mathrm{AF}, \mathrm{AB}, \mathrm{BE} ; \mathrm{BC}, \mathrm{CG} ; \mathrm{BH}, \mathrm{DH}$ | $\mathrm{M} 1 ; \mathrm{A} 1 ; \mathrm{A} 1$ <br> (3) |  |
|  |  |  | B1 |
| (b) |  |  | (1) |
|  |  |  |  |

## Notes for Question 2

a1M1: First three arcs correctly chosen in order (AF, $\mathrm{AB}, \mathrm{BE}, \ldots$ ) or first four nodes correctly chosen in order (A, F, B, E, ...). If any rejections seen at any point then M1 (max) only. Order of nodes may be seen on the top of the table $\{1,3,-,-, 4,2,-,-\}$. If only the weights of the arcs are stated then withhold this mark
a1A1: First five arcs correctly chosen in order (AF, AB, BE, BC, CG, ...) or all eight nodes correctly chosen in order (A, F, B, E, C, G, H, D). Order of nodes may be seen on the top of the table $\{1,3,5,8,4,2,6,7\}$ - do not condone any missing numbers so, for example, the 8 must be above D
a2A1: CSO - all arcs correctly stated and chosen in the correct order. Candidates must be considering arcs for this final mark (do not accept a list of nodes or numbers across the top of the table unless the correct list of arcs (in the correct order) is also seen)

Misread: Starting at a node other than A scores M1 only - must have the first three arcs (or four nodes or four numbers) correct (and in the correct order) - condone any rejections seen for this mark
b1B1: CAO (condone lack of weights on arcs)
c1B1: CAO (condone lack of units)

For reference: $\mathrm{AF}(23), \mathrm{AB}(27), \mathrm{BE}(20), \mathrm{BC}(24), \mathrm{CG}(26), \mathrm{BH}(28), \mathrm{DH}(30)$

| Question <br> Number | Scheme | Marks |
| :---: | :---: | :---: |
| 3. (a) | Alternating path: $\mathrm{A}-6=\mathrm{D}-2=\mathrm{C}-5=\mathrm{F}-4$ <br> Change status: $\quad \mathrm{A}=6-\mathrm{D}=2-\mathrm{C}=5-\mathrm{F}=4$ <br> Improved matching: $A=6, B=1, C=5, D=2$, ( E unmatched), $\mathrm{F}=4$ | M1  <br> A1  <br> A1 (3) |
| (b) | e.g. A is only allocated to task 6 (so A must do task 6), so D must therefore be matched to task 2 (as D can only be allocated to tasks 2 and 6) which leaves E without a match (as E can only be allocated to task 2) - so there are three workers that can only do two tasks | B1 (1) |
| (c) | Alternating path: $\mathrm{E}-2=\mathrm{D}-6=\mathrm{A}-1=\mathrm{B}-3$ or <br> Change status: $\mathrm{E}-2=\mathrm{D}-6=\mathrm{A}-1=\mathrm{B}-5=\mathrm{C}-3$ $\mathrm{E}=2-\mathrm{D}=6-\mathrm{A}=1-\mathrm{B}=3$ <br> or $\mathrm{E}=2-\mathrm{D}=6-\mathrm{A}=1-\mathrm{B}=5-\mathrm{C}=3$ <br> Complete matching: or $A=1, B=5, C=3, D=6, E=2, F=4$ | M1 <br> A1 <br> A1 <br> (3) <br> 7 marks |
| Notes for Question 3 |  |  |
| a1M1: A <br> a1A1: C <br> a2A1: C <br> five arcs <br> b1B1: fo argumen or there <br> - A <br> - A <br> - 1, <br> - 2 <br> - B <br> - T <br> - A <br> - A | alternating path from A to 4 (or vice-versa) <br> O - a correct path including change status either stated or shown. Chosen path O (improved matching) must follow from the correct stated path. Accept on a cl nly) <br> this mark tasks/workers must be referred to explicitly by number/letter - the two are those that state that there are three workers (A, D and E) that can only do two four tasks (1, 3, 4 and 5) that can only be done by three workers (B, C and F). <br> can only do 6, D can only do 2 and 6, and E can only do $2-$ B1 D and E between them can only do 2 and $6-\mathrm{B} 1$ , 4 and 5 can only be done by $\mathrm{B}, \mathrm{C}$ and $\mathrm{F}-\mathrm{B} 1$ nd 6 can only be done by A, D and E-B0 C and F can only do $1,3,4$ and $5-\mathrm{B} 0$ ere are three workers that can only do two tasks - B0 can only do $6, \mathrm{E}$ can only do 2 therefore D has no task to do -B 0 must do 6 , E must do 2 so therefore D has no task to do as D can only do 6 and | r <br> diagram (with <br> ost common asks (2 and 6) example, <br> bod B1 |
| c1M1: <br> c1A1: <br> c2A1: <br> must ha | alternating path from E to 3 (or vice-versa) <br> - a correct path including change status stated or shown. Chosen path clear (complete matching) must follow from two correct stated paths (so both previo been awarded). Accept on a clear diagram (with six arcs only) | M marks |
| Misread: Alternating path from A to 3 in (a) - mark both parts (a) and (c) as a misread (so remove the final two A marks if earned - so can score a maximum of M1A1A1 in (a) and M1A0A0 in (c)) |  |  |
| In (a) Alternating path is $\mathrm{A}-6=\mathrm{D}-2=\mathrm{C}-3$ leading to $\mathrm{A}=6, \mathrm{~B}=1, \mathrm{C}=3, \mathrm{D}=2$, ( E unmatched), $\mathrm{F}=5$ In (c) (i) $\mathrm{E}-2=\mathrm{D}-6=\mathrm{A}-1=\mathrm{B}-5=\mathrm{F}-4$ or (ii) $\mathrm{E}-2=\mathrm{D}-6=\mathrm{A}-1=\mathrm{B}-3=\mathrm{C}-5=\mathrm{F}-4$ leading to to (i) $\mathrm{A}=1, \mathrm{~B}=5, \mathrm{C}=3, \mathrm{D}=6, \mathrm{E}=2, \mathrm{~F}=4$ or (ii) $\mathrm{A}=1, \mathrm{~B}=3, \mathrm{C}=5, \mathrm{D}=6, \mathrm{E}=2, \mathrm{~F}=4$ |  |  |
| If alternating path in (a) starts from E then send to review |  |  |


| Question Number | Scheme |  |  |  |  |  |  |  | Marks |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 4. (a) | $\frac{178}{45}=3.95 \ldots$ so lower bound is 4 bins |  |  |  |  |  |  |  | M1 A1 | (2) |
| (b) | Bin 1: 23 18 <br> Bin 2: 27 9 <br> Bin 3: 25 10 <br> Bin 4: 12  <br> Bin 5: 24   |  |  |  |  |  |  |  | M1 A | (2) |
| (c) | e.g. (left to right) |  |  |  |  |  |  |  | M1 |  |
|  | 23 18 | 27 | 9 | 25 | 10 | 12 | 30 | 24 |  |  |
|  | $23-27$ | 18 | 25 | 10 | 12 | 30 | 24 | 9 |  |  |
|  | $27-23$ | 25 | 18 | 12 | 30 | 24 | 10 | 9 | A1 |  |
|  | $27-25$ | 23 | 18 | 30 | 24 | 12 | 10 |  |  |  |
|  | 27 25 | 23 | 30 | 24 | 18 | 12 | 10 | 9 | $\mathrm{A} 1 \mathrm{ft}$ |  |
|  | $27-25$ | 30 | 24 | 23 | 18 | 12 | 10 | 9 |  |  |
|  | 27 30 | 25 | 24 | 23 | 18 | 12 | 10 | 9 | A1cso | (4) |
|  | $30-27$ | 25 | 24 | 23 | 18 | 12 | 10 | 9 |  |  |
|  | List in order |  |  |  |  |  |  |  |  |  |
| (d) |  |  |  |  |  |  |  |  | M1 A1 | (2) |
| (e) |  |  |  |  |  |  |  |  | B1 <br> 11 ma |  |
| Notes for Question 4 |  |  |  |  |  |  |  |  |  |  |
| a1M1: Attempt to find the lower bound $(178 \pm 30) / 45$ (a value of 3.95 or 3.96 seen with no working can imply this mark) <br> a1A1: CSO - correct calculation seen or 3.95 or 3.96 followed by $4-$ accept 3.9 if correct calculation seen. An answer of 4 with no working scores M0A0 <br> b1M1: First six items placed correctly - condone cumulative totals for M1 only <br> b1A1: CSO - all correct |  |  |  |  |  |  |  |  |  |  |


| Question <br> Number | Scheme | Marks |
| :---: | :---: | :---: |
| c1M1: Bubble sort Consistent direction throughout sort, end number (greatest/least) in place and first pass |  |  |

c1M1: Bubble sort. Consistent direction throughout sort, end number (greatest/least) in place and first pass correct
c1A1: Second and third passes correct - so end three numbers in place
c2A1ft: Fourth and fifth passes correct following through from the candidate's third pass - so end five numbers in place
c3A1: CSO (correct solution only) - including either a 'sort complete' statement (after the seventh pass) or final list rewritten/eighth pass

Sorting list into ascending order in (c)

- If the candidate sorts the list into ascending order and reverses the list in (c) then they can score full marks
- If the list is not reversed then mark as a misread (so remove the last two A marks earned). If the candidate says that the list needs reversing but doesn't actually show the reversed list then remove the final A mark earned
d1M1: Must be using 'sorted' list in descending order. First six items placed correctly. Condone cumulative totals for M1 only
d1A1: CSO - all correct
SC for (d) - if 'sorted' list is incorrect from part (c) and M0 would be awarded in (d) then award M1 only in (d) for their first six items correctly placed - by 'incorrect' they can have only one error, e.g. one missing number, one extra number, or one number incorrectly placed
e1B1: CAO - must have used five bins in (d) - an argument based on the fact that 5 of the suitcases weigh more than half of the maximum weight capacity of a container. Allow mention of $>22$ (rather than $>22.5$ )
right to left in (c)

| 23 | 18 | 27 | 9 | 25 | 10 | 12 | 30 | 24 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{3 0}$ | 23 | 18 | 27 | 9 | 25 | 10 | 12 | 24 |
| $\mathbf{3 0}$ | $\mathbf{2 7}$ | 23 | 18 | 25 | 9 | 24 | 10 | 12 |
| $\mathbf{3 0}$ | $\mathbf{2 7}$ | $\mathbf{2 5}$ | 23 | 18 | 24 | 9 | 12 | 10 |
| $\mathbf{3 0}$ | $\mathbf{2 7}$ | $\mathbf{2 5}$ | $\mathbf{2 4}$ | 23 | 18 | 12 | 9 | 10 |
| $\mathbf{3 0}$ | $\mathbf{2 7}$ | $\mathbf{2 5}$ | $\mathbf{2 4}$ | $\mathbf{2 3}$ | 18 | 12 | 10 | 9 |

List in order




| Question <br> Number | Scheme | Marks |
| :---: | :---: | :---: |

## Notes for Question 7

a1M1: All top boxes complete, values generally increasing in the direction of the arrows ('left to right'), condone one 'rogue' value - condone a missing 0 in the first box for the M mark only a1A1: CAO (top boxes)
a2M1: All bottom boxes complete, values generally decreasing in the opposite direction of the arrows ('right to left'), condone one 'rogue' value - condone a missing 0 in the first box for the M mark only a2A1: CAO (bottom boxes)
b1B1: CAO for defining 'critical' part
b2B1: CAO for defining 'path' part
c1B1: CAO (AGIK)
d1B1: CAO - as a minimum accept 'no effect' but not just ' 0 '
d2B1: CAO - as a minimum accept ' 1 day late' or 'finishes at their $27+1$ ' e.g. at time 28 but not just ' 28 '
e1M1: Attempt to find lower bound: (a value in the interval [73-95] / their finish time) or (sum of the activities / their finish time) or as a minimum accept awrt 3.1
e1A1: CAO - either a correct calculation seen or awrt 3.1 then 4 . An answer of 4 with no working is M0A0
f1M1: Not a cascade chart. 4 'workers' used at most and at least 9 activities placed
f1A1: 4 workers. All 15 activities present (just once). Condone at most two errors. An activity can give rise to at most three errors; one on duration, one on time interval and only one on IPA
f2A1: 4 workers. All 15 activities present (just once). No errors

| Activity | Duration | Time interval | IPA |
| :---: | :---: | :---: | :---: |
| A | 7 | $0-7$ | - |
| B | 3 | $0-5$ | - |
| C | 8 | $0-12$ | - |
| D | 1 | $3-7$ | B |
| E | 6 | $7-16$ | A, D |
| F | 6 | $7-16$ | A, D |
| G | 5 | $7-12$ | A, D |
| H | 7 | $3-12$ | B |
| I | 4 | $12-16$ | C, G, H |
| J | 4 | $13-21$ | E |
| K | 11 | $16-27$ | E, F, I |
| L | 4 | $16-22$ | E, F, I |
| M | 7 | $12-22$ | C, G, H |
| N | 6 | $17-27$ | F, I, J |
| P | 5 | $20-27$ | L, M |


| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 8. (a) | $\begin{aligned} & \text { Minimise }(P=) 2 x+3 y+5 z \\ & \text { Subject to: } \\ & x+y+z \geq 50 \\ & y \geq 2 z \\ & \frac{3}{5}(x+y+z) \geq x \text { simplifies to } 2 x \leq 3 y+3 z \\ & \frac{1}{3}(x+y+z) \leq y \text { simplifies to } 2 y \geq x+z \\ & (x, y, z \geq 0) \end{aligned}$ | B1 <br> B1 <br> B1 <br> M1 A1 <br> M1 A1 |
| (b) |  | B1 <br> B1 <br> B1 <br> B1 <br> (4) |
| (c) | Drawing an objective line accept reciprocal gradient Correct objective line minimum length equivalent to $(0,5)$ to $(7.5,0)$ V labelled correctly | M1  <br> A1  <br> A1 (3) |
| (d) | 20 ballpoint pens, 20 rollerball pens (and 10 fountain pens) Cost: (£) 150 | DB1 DB1 (2) 16 marks |

## Notes for Question 8

a1B1: CAO - expression correct and 'minimise'
a2B1: CAO $(x+y+z \geq 50)$
a3B1: CAO $(y \geq 2 z)$
a1M1: Correct method - must see $\frac{3}{5}(x+y+z) \bullet x$ where $\bullet$ is any inequality or $=$. The bracket must be present or implied by later working
a1A1: CAO - simplified - answer must have integer coefficients $(2 x \leq 3 y+3 z)$ - the correct inequality with no working implies M1A1
a2M1: Correct method - must see $\frac{1}{3}(x+y+z) \bullet y$ where $\bullet$ is any inequality or $=$. The bracket must be present or implied by later working
a2A2: CAO - simplified - answer must have integer coefficients $(2 y \geq x+z)$ - the correct inequality with no working implies M1A1

In (b) lines must be long enough to define the correct feasible region and pass through one small 'square' of the points stated in either the horizontal or vertical direction, e.g. for $(90,50)$ the line must pass through a point in the interval [88, 92] for $x$ or $[49,51]$ for $y$ :

- $x+y=40$ from $(0,40)$ to $(40,0)$
- $2 x-3 y=30$ from $(30,10)$ to $(97.5,55)$
- $-x+2 y=10$ from $(0,5)$ to $(90,50)$
- $y=20$ from $(0,20)$ to $(90,20)$
b1B1: Any two lines correctly drawn
b2B1: Any three lines correctly drawn
b3B1: All four lines correctly drawn
b4B1: Region, R, correctly labelled - not just implied by shading - dependent on scoring the first three marks in this part
c1M1: Drawing the correct objective line or its reciprocal. Line must be correct to within one small 'square' if extended from axis to axis in either the horizontal or vertical direction. If their line is shorter than the length equivalent to that of the line from $(0,5)$ to $(7.5,0)$ then M0
c1A1: Correct objective line - same condition that the line must be correct to within one small 'square' if extended from axis to axis in either the horizontal or vertical direction
c2A1: V labelled clearly on their graph. This mark is dependent on all four marks in (b) and the previous A mark in (c). By clearly labelled the vertex should either be labelled ' $V$ ' or circled or clearly distinguishable from any other vertex (but A0 if not clear e.g. another vertex circled too)
d1B1: CAO dependent on full marks in (b) and at least M1A1 in (c) - condone no mention of fountain pens - answer must be in context
d2B1: CAO dependent on full marks in (b) and at least M1A1 in (c) - condone lack of units

